

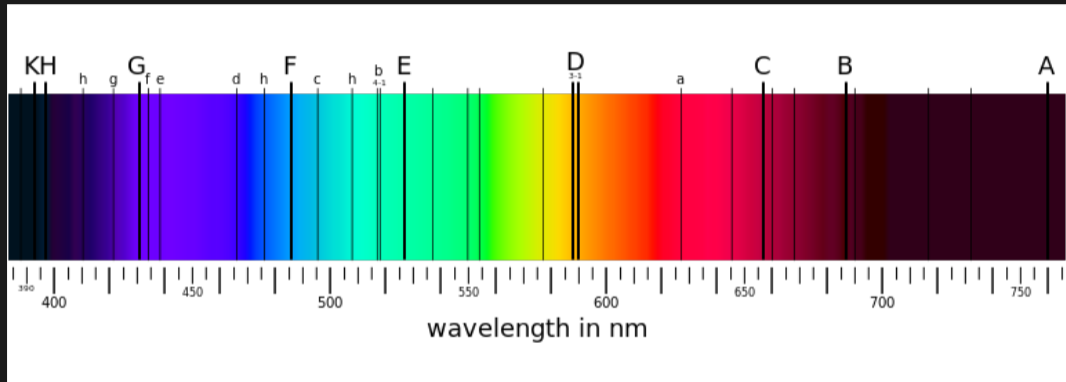
# Robust High-Angular Resolution Astronomy

F. Martinache (+ M.J. Ireland)

May 14, 2018

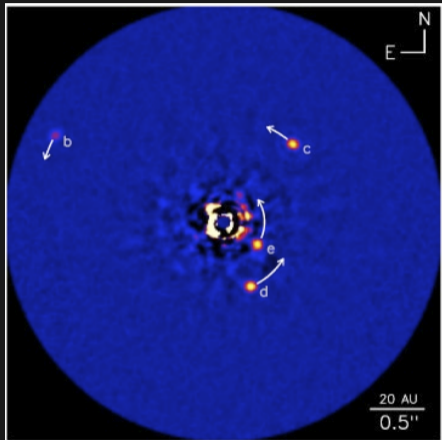


# Stellar Spectroscopy

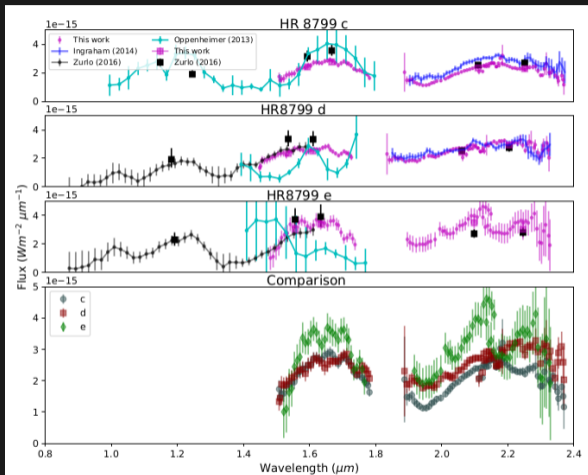


Fraunhofer lines [credit: Wikipedia]

# Extrasolar planets

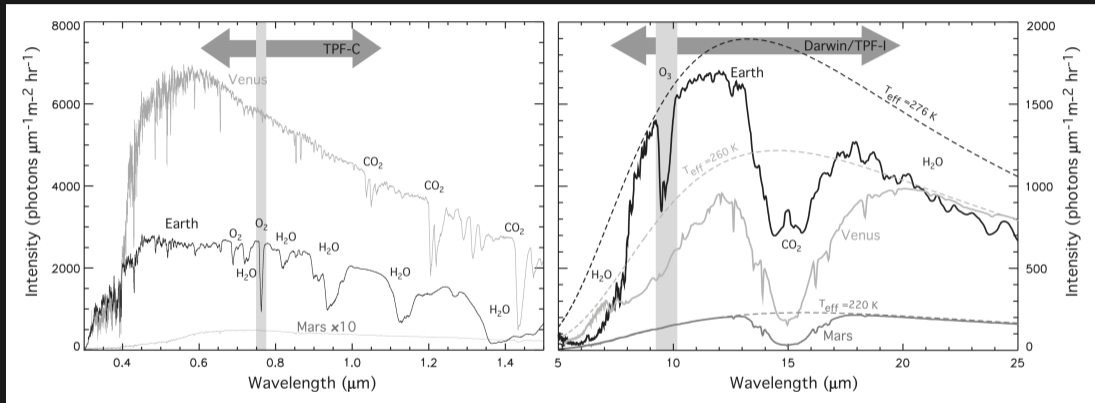


30 Myr old planetary system  
HR8799



Greenbaum et al, 2018.

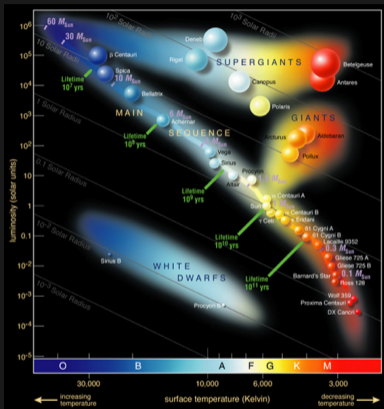
# The ambition: bio-markers!



Selsis et al, 2008.



# A global story of the life of extrasolar planets



[credit: ESO]

- Build a planet equivalent of the HR diagram?
- To tell a story of planet formation and evolution
- Core-accretion and/or gravitational instability start
- Migration tracks?
- Need many unambiguous spectroscopic observations

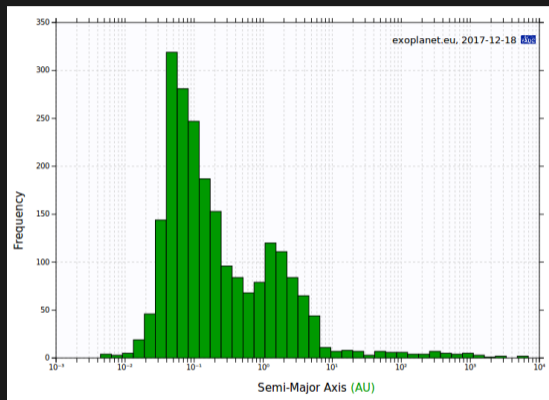
# Earth-Sun equivalent

A Solar system equivalent at 10 pc:

- Earth: 1 AU  $\rightarrow$  100 mas
- Jupiter: 5 AU  $\rightarrow$  500 mas

To be compared to:

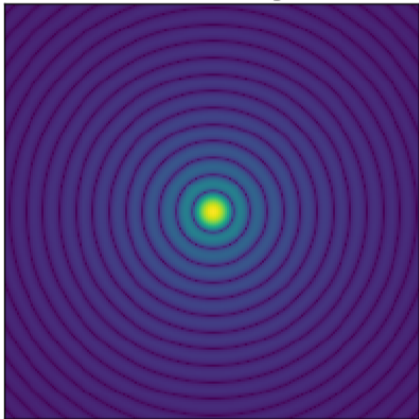
- the diffraction limit
- given by the ratio  $\lambda/D$
- 8-meter ( $1.6 \mu\text{m}$ ): 40 mas
- 100 meter ( $3.6 \mu\text{m}$ ): 5 mas



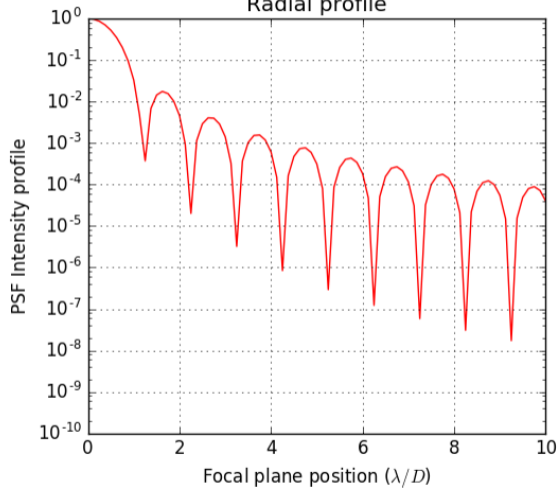
Distribution of known planets semi-major axis

# Physics says OK but hard

Ideal PSF image

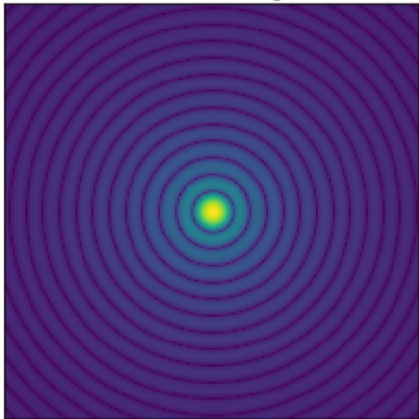


Radial profile

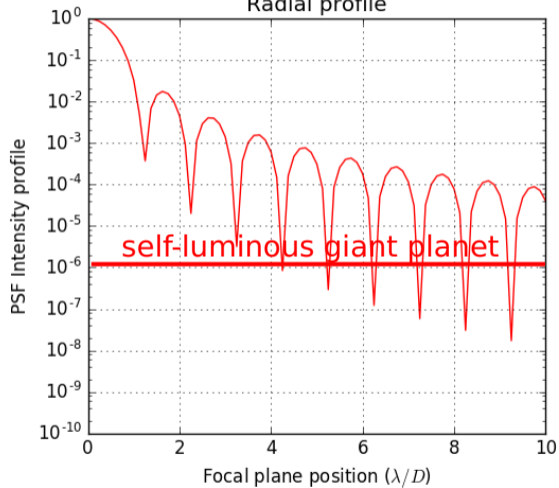


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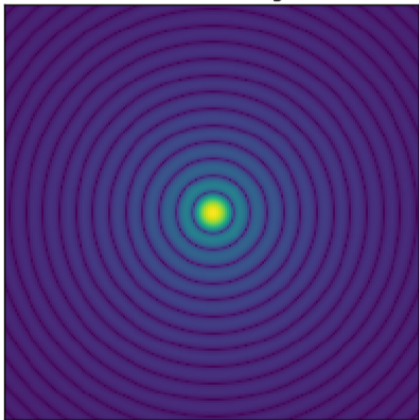


Radial profile

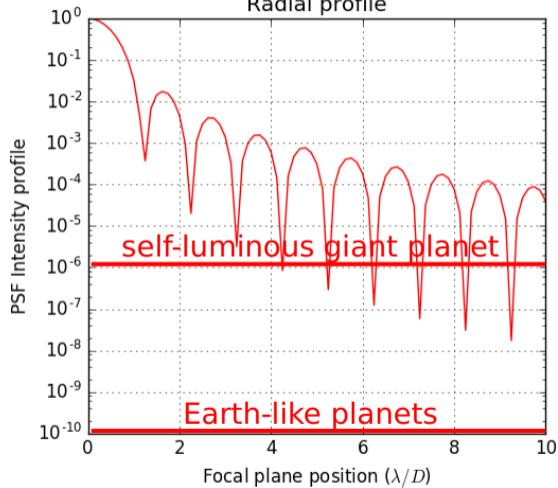


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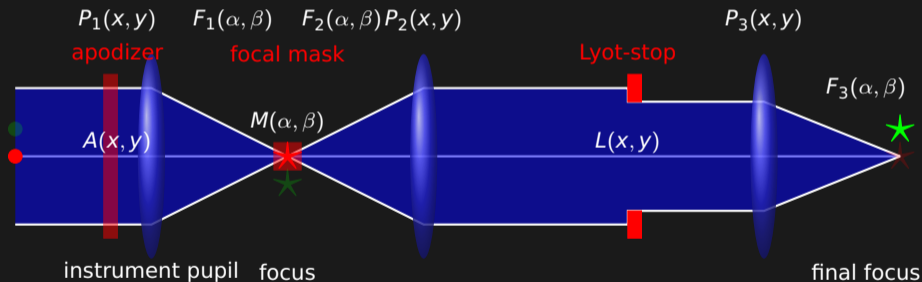


Radial profile



# High-contrast imaging

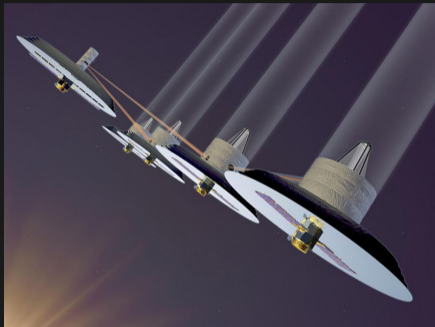
- Reduce the photon noise of the bright source to reveal the faint structures
- Two solutions: coronagraphy and interferometric nulling
- Example: coronagraphy



In both cases, the device suppresses the **static on-axis diffraction pattern**

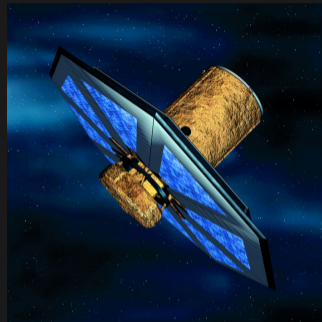
# From incredibly daring to very prudent

[credit: NASA]



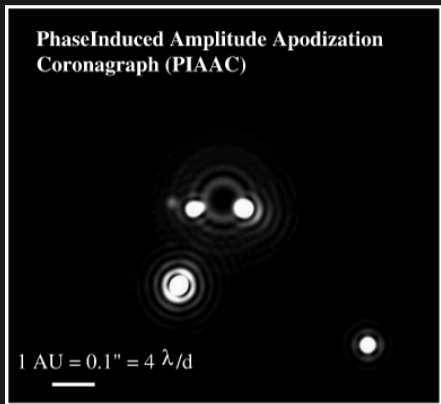
- in 2004: coronagraph and interferometer!
- in 2011: project canceled

[credit: ESA]



- 2004: ESA examines Darwin
- In 2007: concept study closed
- There is no Darwin project today

# Ideal solutions in a non-ideal world

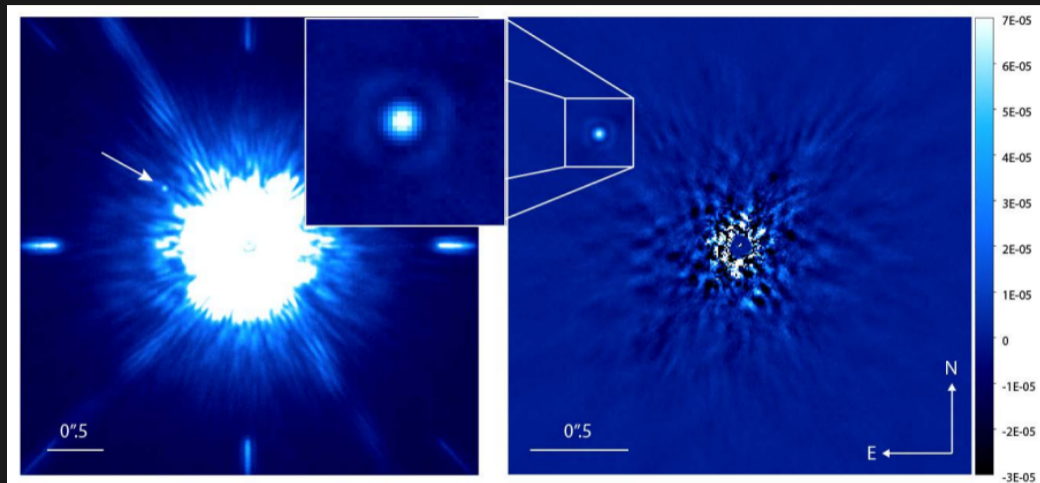


- Optical solutions are available:
  - ▶ e.g: PIAAC and Vortex coronagraphs
- In theory: very high-contrast down to the diffraction limit is possible
- In practice performance dominated by the input **wavefront quality**
- Stability requirement = f(raw contrast):
  - ▶  $\alpha = \lambda \times \sqrt{c}/2\pi$
  - ▶  $c=10^{-6} \rightarrow$  sub-nm wavefront quality
- State of the art:  $\sim 50$  nm ( $\rightarrow c \sim 4 \times 10^{-2}$ )

Guyon et al, 2005, ApJ, 622, 744

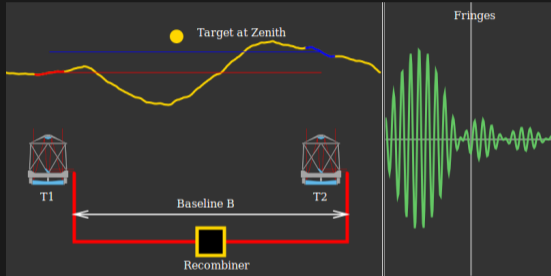


# Operating in an imperfect world



Kühn et al, 2017, PASP, 2018  
Coronagraphy saved by post-processing

# Interferometry: measuring one thing well

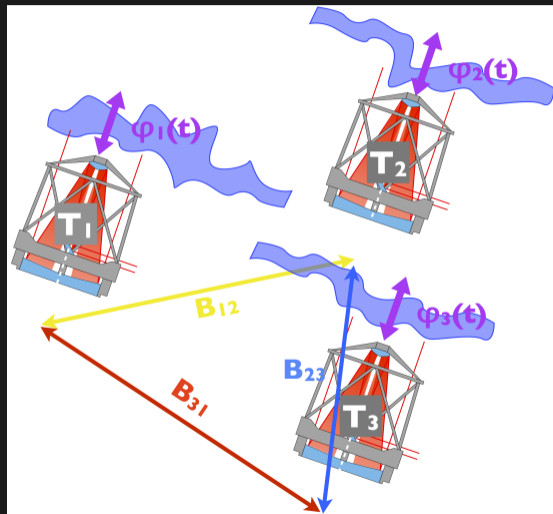


web-link

Measuring the **complex visibility**

- one single complex number
- understand biases and noises
- goes beyond the resolution limit

# Take the environment into account



A special treatment for the phase:

$$\phi(1-2) = \phi_O(1-2) + (\varphi_1 - \varphi_2)$$

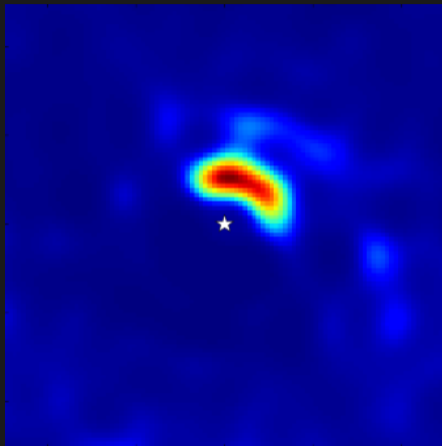
$$\phi(2-3) = \phi_O(2-3) + (\varphi_2 - \varphi_3)$$

$$\phi(3-1) = \phi_O(3-1) + (\varphi_3 - \varphi_1).$$

- **linear perturbation** term
- coupling of the perturbation along multiple baselines
- can find linear combinations that cancel the perturbation

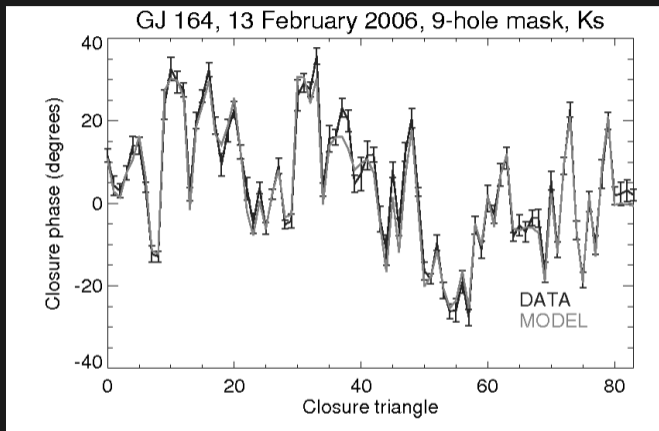
Jennison R.C., 1958.

# Closure-phase



Transition Disk host LkCa 15  
Ireland, 2013, MNRAS, 433, 1718

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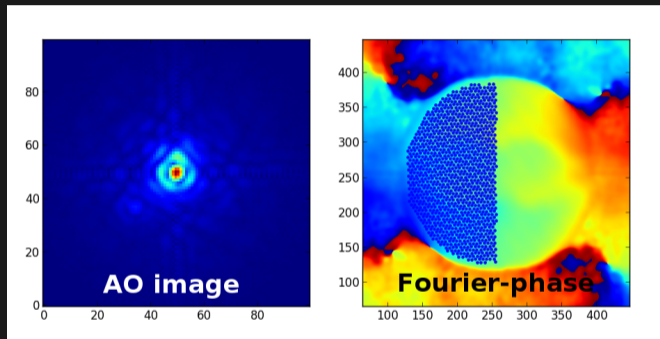
2009: AO-residuals  $\sim 150$  nm RMS  
closure-phase stability  $< 1^\circ$   
roughly corresponds to  $\lambda/1000$

KERNEL: Journée OCA/CdF

May 14, 2018

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# Kernel-phase: beyond the triangle



Martinache, 2010, ApJ, 724, 464

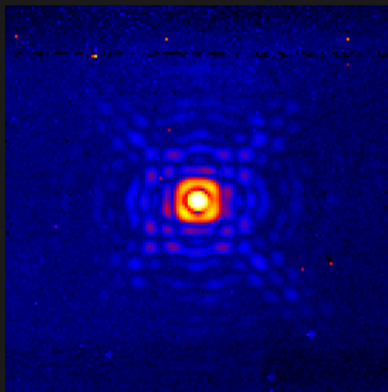
$$I = O \otimes \text{PSF}(t)$$

In the presence of time-varying aberrations, the information at each pixel is degenerate.

There is an sub-space where good observables exist that are robust against first and second order phase residuals.

These observables are called **kernel-phases**

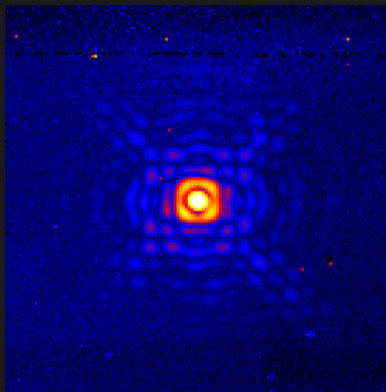
# Use case 1



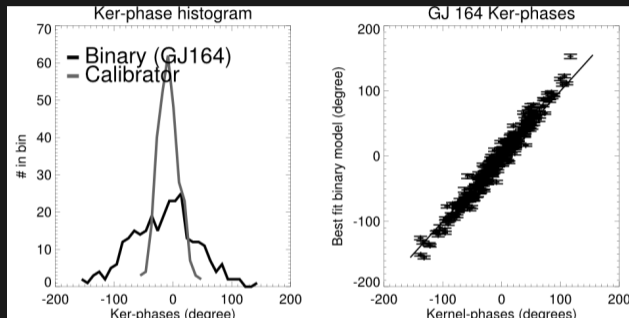
GJ 164 (HST/NICMOS1)

# Use case 1

super-resolution detection is possible



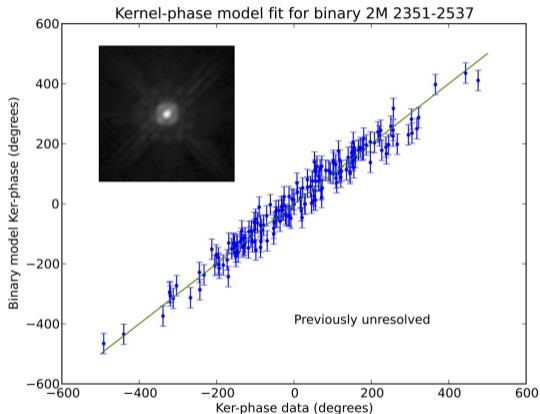
GJ 164 (HST/NICMOS1)



Histogram and kernel model of GJ 164

- companion  $c \sim 10 : 1$  at  $0.5\lambda/D$  detected
- relative astrometry and phot. constraints

## Use case 2



- snapshot survey of  $\sim 80$  L-Dwarfs
- two filters: F110W and F170M
- 10 known visual binaries
- 5 clear new detections
- 4 marginal detections
- separations down to  $\sim 1$  AU

Pope et al, 2013, ApJ, 767, 110



# Phase noise is dead: long live photon noise!

- An **instant phase-noise canceling filter**: powerful tool
- The **photon noise of the bright source** remains
- Reported detections are in the  $\sim 10^{-3}$  contrast range

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- designed for greatness
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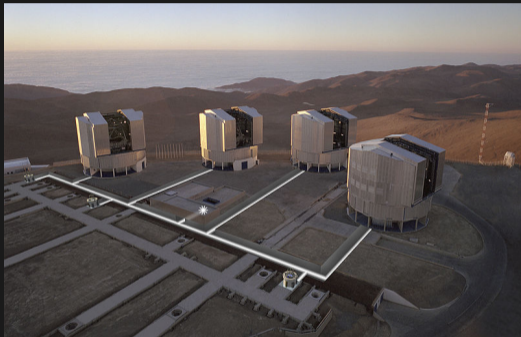
Kernel-phase:

- characterized by its robustness
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## A design principle?

Can we make the ability to produce kernels a guiding principle in the instrument design?

# A simple problem: a 4-telescope interferometer



[VLTi [Credit: ESO]]

Favorable contrast → L-band

Milliarcsec resolution → VLTi

High-contrast → **Nulling**

- Four telescopes: 75 % efficiency
- A finite number of degrees of freedom
- A finite number of covariated quantities
- → The problem can be well posed

# Nulling interferometry

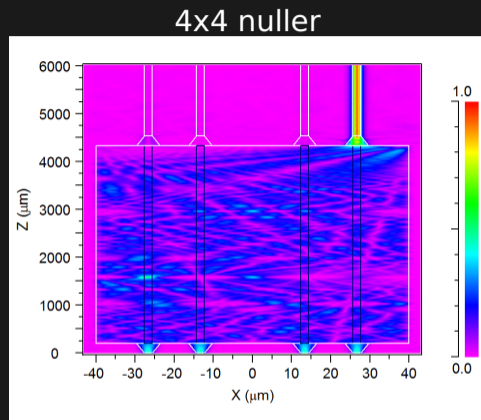
## State of the Art:

- Cancel on-axis light source (Bracewell, 1978):
- Solutions exist for N-aperture interferometers (Guyon et al, 2013)
- Design emphasis: produce **dark (nulled) outputs**
- Like a coronagraph, **rejection is sensitive to environment**
- Post-processing required (e.g. Null Self-calibration, Hanot et al, 2011)
- Keck and LBTI

# 4T nuller for VLT!

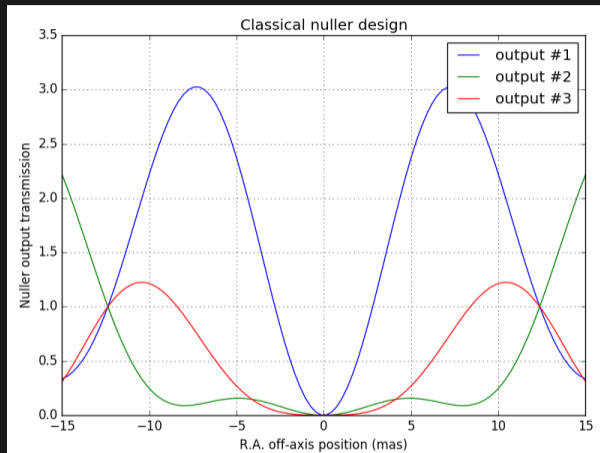
$$\mathbf{N} = 0.5 \times \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & 1 & -1 \\ 1 & -1 & -1 & 1 \end{bmatrix}$$

- Four telescope inputs
- One bright output
- Three dark outputs



(MMI design by Harry-Dean Kenchington  
Goldsmith, ANU PhD candidate)

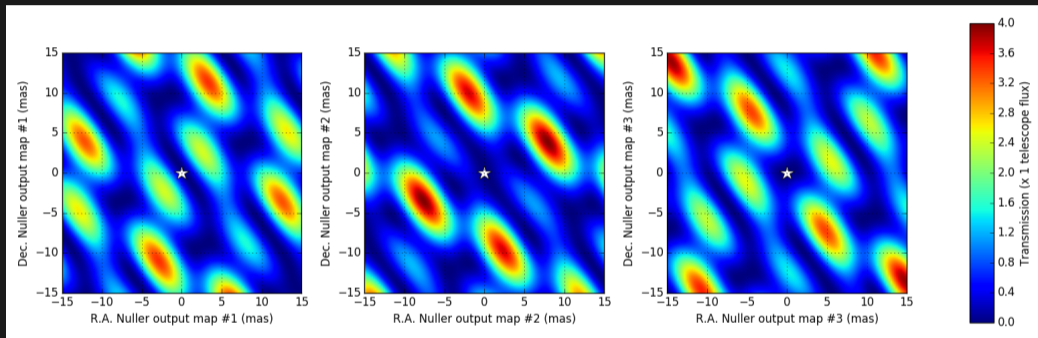
# Quadratic output (for an inline interferometer)



The effect of the perturbation is degenerate  
The behavior is the same for photometric perturbations

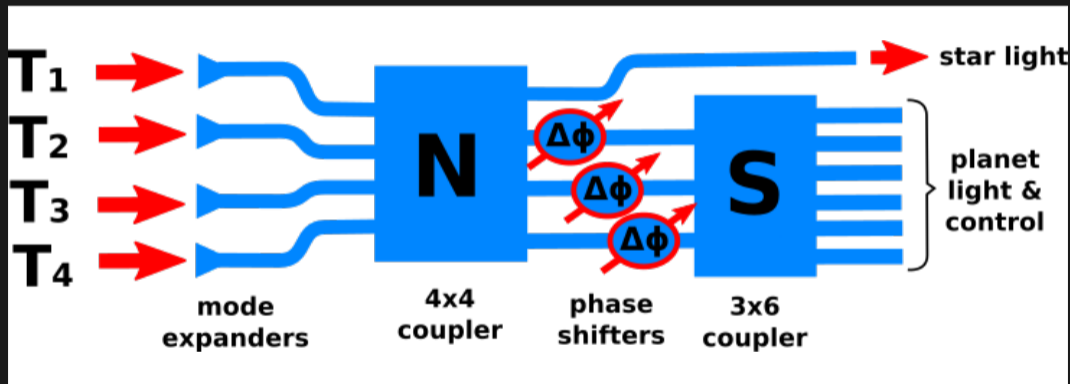


# 4T-Nuller: On-sky response for VLTI



Only at zenith!

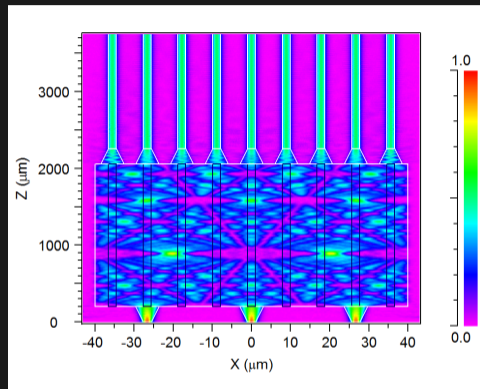
# Modify the nuller



To asymmetrize the perturbation dependance of the nuller!

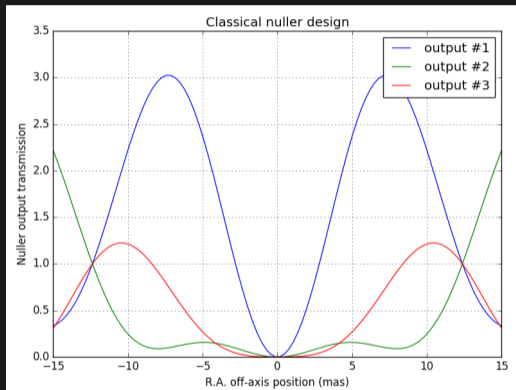
# Modified 4T-Nuller: principle

$$\mathbf{S} = \frac{1}{\sqrt{4}} \times \begin{bmatrix} 1 & e^{i\theta} & 0 \\ -e^{-i\theta} & 1 & 0 \\ 1 & 0 & e^{i\theta} \\ -e^{-i\theta} & 0 & 1 \\ 0 & 1 & e^{i\theta} \\ 0 & -e^{-i\theta} & 1 \end{bmatrix}$$

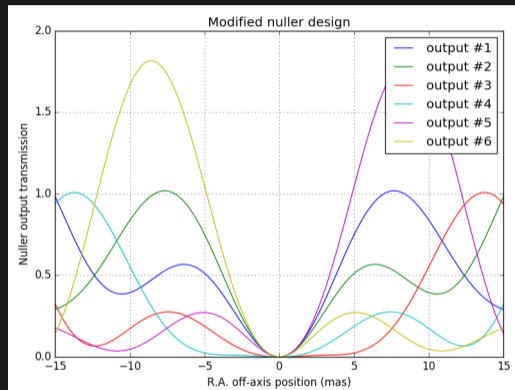


(MMI design by Harry-Dean Kenchington Goldsmith, ANU PhD candidate)

# Break the symmetry

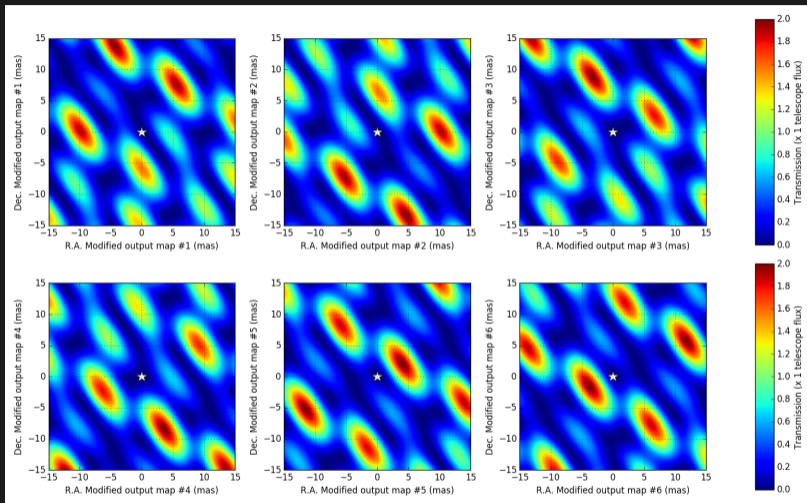


Classical design



Modified design

# Modified 4T-Nuller: on-sky response for VLT



From 3 to 6 outputs

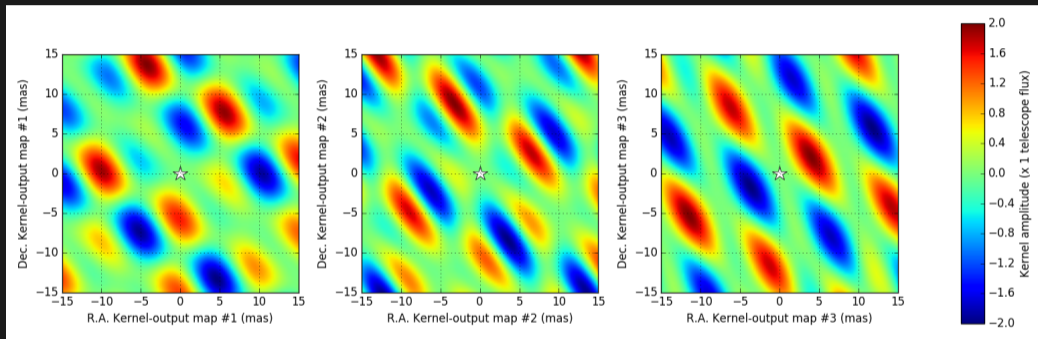
# Kernel-nulled outputs

- Unlike kernel-phase, no first order dependence on piston errors
- Nuller error dominated by second order errors

$$\delta \mathbf{l} = \mathbf{A} \times \left[ \frac{\partial^2 \mathbf{l}}{\partial \varphi_1^2}, \frac{\partial^2 \mathbf{l}}{\partial \varphi_2^2}, \frac{\partial^2 \mathbf{l}}{\partial \varphi_3^2}, \frac{\partial^2 \mathbf{l}}{\partial \varphi_1 \partial \varphi_2}, \frac{\partial^2 \mathbf{l}}{\partial \varphi_1 \partial \varphi_3}, \frac{\partial^2 \mathbf{l}}{\partial \varphi_2 \partial \varphi_3} \right]^T. \quad (1)$$

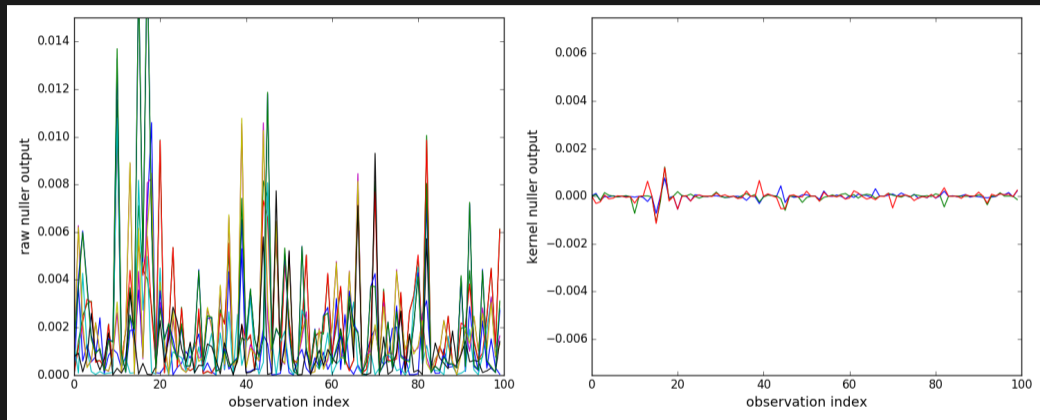
- record a new 2<sup>nd</sup> order perturbation response matrix  $\mathbf{A}$
- and find a kernel for this matrix

# Kernel-Nullled outputs: on-sky response for VLTI



Maps are anti-symmetric! A single snapshot observation can constrain a companion's position.

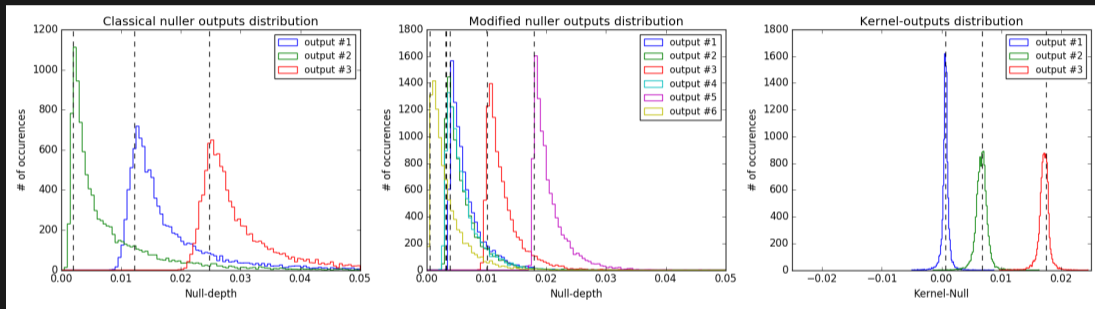
# Kernel-Nullled outputs: enhanced stability



50 nm RMS random piston error for the array  
Same vertical scale for raw (left) and kernel (right) outputs.  
The kernel-outputs indeed provide additional filtering

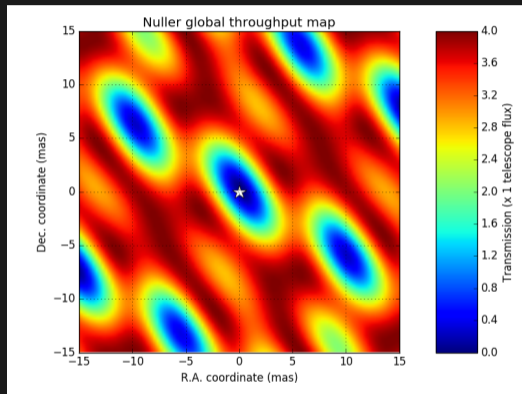


# Kernel-nulled outputs: more robust against piston

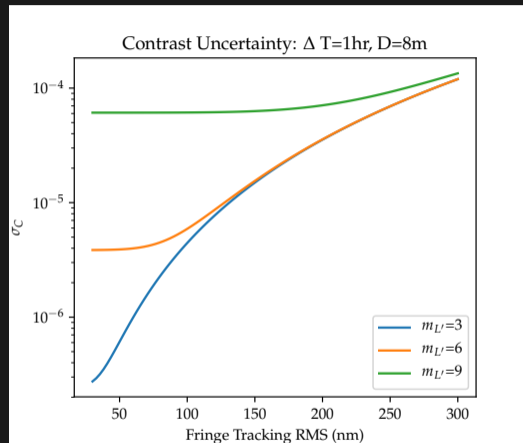


And incidentally, also robust against photometric fluctuations!

# L-band VLTI 4UT



Non-uniform response over the field of view



Median contrast uncertainty

# VIKiNG: the VLT Infrared Kernel NullinG

Two VIKiNG raids:

- Blind survey of potential young hosts using 4 ATs
- Targeted survey of known planets at thermal equilibrium with their host using the 4 UTs for max sensitivity

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Using [exoplanet.eu](http://exoplanet.eu) database and assuming Neptune-like density planet at thermal equilibrium:

- semi-major + distance  $\rightarrow$  angular separation + T
- mass + density + T  $\rightarrow$  planet radius  $\rightarrow$  luminosity
- contrast cut-off  $> 10^{-5}$ : 14 targets make the cut
- angular separation range from 5 to 12 mas
- 14 planets detectable in  $< 2$  hours (SNR=5) with UTs

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Catalogue

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GJ 86 A b  
BD+20 2457 b  
HD 110014 c  
11 Com b  
ksi Aql b  
61 Vir b  
HIP 105854 b  
HIP 107773 b  
mu Ara c  
nu Oph b  
HD 168443 b  
HIP 67851 b  
HD 69830 b  
HD 16417 b

# Thank you

## Kernel-nulling

The power of Thor's hammer (the nuller) now driven with surgical precision and accuracy (the kernel): the weapon of choice for any VIKiNG aiming to discover new lands!

Please check out our paper:  
<https://arxiv.org/abs/1802.06252>



[Image Credit: <http://www.kungfury.com/>]